## $\underbrace{\overline{\bar{\sigma}}}_{\text {NectPreparation }}$

## Kinetic Theory Important Questions With Answers

NEET Physics 2023

1. Air inside a closed container is saturated with water vapour The air pressure is $p$ and the saturated vapour pressure of water is $\bar{p}$. if the mixture is compressed to one half of its volume by maintaining temperatures constant, the pressure becomes ;
a) $2(p+\bar{p})$
b) $2 p+\bar{p}$
C) $\frac{(p+\bar{p})}{2}$
d) $p+2 \bar{p}$
2. A closed vessel $A$ having volume $V$ contains $N_{2}$ at pressure $P$ and temperature $T$. Another closed vessel $B$ having the same volume V contains He at the same pressure P but temperature 2T. The ratio of masses of $\mathrm{N}_{2}$ and He in the vessels $A$ and $B$ is
a) $1: 2$
b) $3: 2$
c) $5: 2$
d) $14: 1$

## Solution:-

$P=\frac{m_{N 2}}{M_{N 2}} \times \frac{R T}{V}$
$P=\frac{m_{H e}}{M_{H e}} \times \frac{R(2 T)}{V}$
$\therefore \frac{m_{N 2}}{28 \times 10^{-3}} \times \frac{R T}{V}=\frac{m_{H e}}{4 \times 10^{-3}} \times \frac{R T \times 2}{V}$
$\therefore \frac{m_{N 2}}{m_{H e}}=\frac{28}{4} \times 2=\frac{14}{1}$
3. At a given volume and temperature the pressure of a gas:
a) varies inversely as its mass
b) varies inversely as the square of its mass
c) varies linearly as its mass
d) is independent of its mass

## Solution:-

$P=\frac{1}{3}\left(\frac{m N}{V}\right) V^{\overline{2}}$
$p \infty m N$
4. If the intermolecular forces vanish away, the volume occupied by the molecules contained in 4.5 kg water at STP will be given by:
a) $5.6 \mathrm{~m}^{3}$
b) $4.5 \mathrm{~m}^{3}$
c) $11.2 \mathrm{~m}^{3}$
d) $5.6 \mathrm{~m}^{3}$

## Solution : -

When intermolecular force vanishes, the liquid is converted into vapours. Molecular mass of water va pours $=18$ $\mathrm{g}=18 \times 10^{-3} \mathrm{k}$
Now, $18 \times 10^{-3} \mathrm{~kg}$ of water vapour occupies at STP a volume of 22400 cc or 22.4 litre $=22.4 \times 10^{-3} \mathrm{~m}^{3}$
Hence, 4.5 kg occupies
$=\frac{22.4 \times 10^{-3}}{18 \times 10^{-3}} \times 4.5=5.6 \mathrm{~m}^{3}$
5. Two monoatomic ideal gases $A$ and $B$ occupying the same volume $V$, are at the same temperature $T$ and pressure $P$. If they are mixed, the resultant mixture has volume $V$ and temperature $T$. The pressure of the mixture is:
a) $P$
b) $\frac{P}{2}$
c) $4 P$
d) $\mathbf{2 P}$

## Solution:-

Number of moles is conseved.
$\therefore \mathrm{n}_{\mathrm{A}}+\mathrm{n}_{\mathrm{B}}=\mathrm{nmix}$
Where $\mathrm{nA}, \mathrm{nB}$ and nmix represent the number of moles of gas $\mathrm{A}, \mathrm{B}$ and their mixture respectively.
Using ideal gas equation, we get
$\frac{P_{A} V_{A}}{R T_{A}}+\frac{P_{B} V_{B}}{R T_{B}}=\frac{P_{\text {mixture }} V_{\text {mixture }}}{R T_{\text {mixture }}}, \frac{P V}{R T}+\frac{P V}{R T}=\frac{P_{\text {mixture }} V}{R T}$
or $\mathrm{P}_{\text {mixture }}=2 \mathrm{P}$
6. In two vessels of same volume atomic hydrogen and helium at pressure of 1 atm and 2 atm are filled. If temperature of both the samples is same, then average speed of hydrogen atom (UH) will be related to helium (UHe) as:
a) $\left\langle v_{H}\right\rangle=\sqrt{2}\left\langle v_{H e}\right\rangle$
b) $\left\langle v_{H}\right\rangle=\left\langle v_{H e}\right\rangle$
c) $\left\langle v_{H}\right\rangle=2\left\langle v_{H e}\right\rangle$
d) $\left\langle v_{H}\right\rangle=\left\langle v_{H e} / 2\right\rangle$
7. The relation between rms velocity, $\mathrm{v}_{\mathrm{rms}}$ and the most probable velocity , $\mathrm{v}_{\mathrm{rmp}}$, of a gas is:
a) $v_{r m s}=v_{m p}$
b) $\mathbf{v}_{\mathrm{rms}}=\sqrt{\frac{3}{2}} \mathbf{v}_{\mathrm{mp}}$
c) $\mathbf{v}_{\mathrm{rms}}=\sqrt{\frac{2}{3}} \mathbf{v}_{\mathrm{mp}}$
d) $v_{\text {rms }}=\frac{2}{3} v_{m p}$

## Solution : -

$v_{r m s}=\sqrt{\frac{3 K T}{m}}, v_{m p}=\sqrt{\frac{2 K T}{m}}$
$\frac{u_{r m s}}{u_{m p}}=\sqrt{\frac{3}{2}}$
8. A mixture of2 moles of helium gas (atomic mass $=4 \mathrm{amu}$ ) and 1 mole of argon gas (atomic mass $=40 \mathrm{amu}$ ) is kept at 300 K in a container. The ratio of the rms speed
$\left[\frac{v_{r m s}(\text { helium })}{v_{r m s}(\text { argon })}\right]$ is:
a) 0.32
b) 0.45
c) 2.24
d) 3.16

## Solution : -

$v_{r m s}=\sqrt{\frac{3 R T}{M}}$
$\therefore$ Required ratio $=\sqrt{\frac{3 R T}{M}} \quad \sqrt{\frac{M_{A r}}{M_{H e}}}=\sqrt{\frac{40}{4}}=\sqrt{10}=3.16$
9. An ideal gas is
a) one which consists of massless particles
b) one satisfying assumption of kinetic theory
c) a gas consisting small particles
d) one that consists of molecules

## Solution :-

An ideal gas is one which satisfy assumption of kinetic theory.
10. Some gas at 300 K is enclosed in a container. Now the container is placed on a fast moving jet.While the jet is in motion, the temperature of gas
a) rises above 300 K
b) falls below 300 K
c) remains unchanged
d) becomes unsteady

## Solution : -

Motion of particle due to train is ordered motion.Motion of gas molecule in container is disordered motion.Its disordered motion causes change in temperature.In this case, the ordered motion of gas molecules remain unaffected.So, temperature will remain same.
11. Two gases of equal mass are in thermal equilibrium. If $P_{a}, P_{b}$ and $V_{a}$ and $V_{b}$ are their respective pressures and volumes, then which relation is true?
a) $\mathrm{P}_{\mathrm{a}} \mathrm{V}_{\mathrm{a}}=\mathrm{P}_{\mathrm{b}} \mathrm{V}_{\mathrm{b}}$
b) $\mathrm{P}_{\mathrm{a}} / \mathrm{V}_{\mathrm{a}}=\mathrm{P}_{\mathrm{b}} / V_{b}$
c) $\mathrm{P}_{\mathrm{a}}=\mathrm{P}_{\mathrm{b}} ; \mathrm{V}_{\mathrm{a}} \neq \mathrm{V}_{\mathrm{b}}$
d) $\mathrm{P}_{\mathrm{a}} \neq \mathrm{P}_{\mathrm{b}} ; \mathrm{V}_{\mathrm{a}} \neq \mathrm{V}_{\mathrm{b}}$
12. The temperature at which protons in proton gas would have enough energy to overcome Coulomb barrier of 4.14 $\times 10^{-14}$ is (Boltzmann constant $1.38 \times 10^{-23} \mathrm{JK}^{-1}$ )
a) $\mathbf{2 \times 1 0 ^ { 9 }} \mathrm{K}$
b) $10^{9} \mathrm{~K}$
c) $6 \times 10^{9} \mathrm{~K}$
d) $3 \times 10^{9} \mathrm{~K}$
e) $4.510^{9} \mathrm{~K}$

## Solution:-

The temperature at which protons in a proton gas would have enough energy to overcome coulomb barrier between them is given by :
$\frac{3}{2} \mathrm{k}_{\mathrm{B}} \mathrm{T}=\mathrm{K}^{\mathrm{av}}$ $\qquad$
Where $K_{a v}$ is the average Kinetic energy of the proton, $T$ is the temperature of the proton gas and $K_{B}$ is the Boltzmann's constant From eqn, (i) we get
$T=\frac{2 K_{a v}}{3 K_{B}}$
Substituting the values, we get;
$T=\frac{2 \times 4.14 \times 10^{-14} \mathrm{~J}}{3 \times 1.38 \times 10^{-23} J K^{-1}}=2 \times 10^{9} \mathrm{~K}$
13. A thermally insulated vessel contains an ideal gas of molecular mass $M$ and ratio of specific heats $\gamma$. It is moving with speed $v$ and is suddenly brought to rest.Assuming no heat is lost to the surroundings, its temperature increases by
a) $\frac{(\gamma-1)}{2 R} M v^{2} K$
b) $\frac{(\gamma-1)}{2(\gamma+1) R} M v^{2} K$
c) $\frac{(\gamma-1)}{2 \gamma R} M v^{2} K$
d) $\frac{\gamma M v^{2}}{2 R} K$

## Solution:-

Work done (W) in bringing the vessel at rest is equal to change in internal of gas ( $\Delta \mathrm{U}$ )
So, $\mathrm{W}=\Delta \mathrm{U}$
$\Rightarrow \frac{1}{2} m v^{2}=n C_{v} d T$
$\Rightarrow \frac{1}{2} m v^{2}=\frac{m}{M} \frac{R}{\gamma-1} d T$
$\Rightarrow d T=\frac{M(\gamma-1) v^{2}}{2 R}$ kelvin
$d T=\frac{\gamma-1}{2 R} M v^{2}$ kelvin
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15. The mean square speed of 4 molecules of a gas having speeds $1,2,3$ and $4 \mathrm{~m} / \mathrm{s}$ is
a) $2.44 \mathrm{~m} / \mathrm{s}$
b) $7.5 \mathrm{~m} / \mathrm{s}$
c) $2.5 \mathrm{~m} / \mathrm{s}$
d) $9 \mathrm{~m} / \mathrm{s}$
16. A container has $N$ molecules at absolute temperature $T$. If the number of molecules is doubled but kinetic energy in the box remains the same as before, the absolute temperature of the gas is:
a) T
b) $\mathrm{T} / 2$
c) 2 T
d) zero

## Solution:-

$\overline{K E}=\frac{3}{2} \mathrm{kT}$
On doubling the number of molecules and keeping total KE same, average $\mathrm{KE}(\overline{\mathrm{KE}})$ becomes half, resulting in half the temperature.
17. Consider I cc sample of air at absolute temperature To at sea level and another 1 cc sample of air at a height, where pressure is one-third atmosphere.The absolute temperature T of the sample at the height is:
a) equal to ( $T_{0} / 3$ )
b) equal to ( $3 / \mathrm{T}_{0}$ )
c) equal to $T_{o}$
d) cannot be determind in terms of $\mathrm{T}_{0}$ from the above data

## Solution:-

Mass of 1 cc of gas at sea level and at given height does not remain the same and gas laws hold good only for a constant mass.
18. Internal energy of $n_{1}$ mole of hydrogen at temperature $T$ is equal to internal energy of $n_{2}$ mole of helium at temperature 2 T.Then, ratio $\frac{n_{1}}{n_{2}}$ is
a) $\frac{3}{2}$
b) $\frac{2}{3}$
c) $\frac{6}{5}$
d) $\frac{3}{7}$

## Solution : -

Internal energy of n moles of an ideal gas at temperature T is given by
$\mathrm{U}=\frac{f}{2} \mathrm{nRT} \quad$ ( f is degree of freedom)
$\mathrm{U}_{1}=\mathrm{U}_{2}$
$\mathrm{f}_{1} \mathrm{n}_{1} \mathrm{~T}_{1}=\mathrm{f}_{2} \mathrm{n}_{2} \mathrm{~T}_{2}$
$\frac{n_{1}}{n_{2}}=\frac{f_{2} T_{2}}{f_{1} T_{1}}=\frac{(3)(2)}{(5)(1)}=\frac{6}{5}$
$f_{1}$ is degree of freedom of $H=5$
$\mathrm{f}_{2}$ is degree of freedom of $\mathrm{He}=3$
19. Two containers of equal volume contain the same gas at the pressures $p_{1}$ and $p_{2}$ and absolute temperatures
$T_{1}$ and $T_{2}$ respectively. On joining vessels, the gas reaches a common pressure $p$ and a common temperature
T.The ratio of $\mathrm{p} / \mathrm{T}$ is
a) $\frac{p_{1} T_{2}+p_{2} T_{2}}{T_{1} \times T_{2}}$
b) $\frac{p_{1} T_{2}+p_{2} T_{2}}{T_{1}+T_{2}}$
c) $\frac{1}{2}\left[\frac{p_{1} T_{2}+p_{2} T_{1}}{T_{1} T_{2}}\right]$
d) $\frac{p_{1} T_{2}-p_{2} T_{2}}{T_{1} \times T_{2}}$

## Solution : -

For a closed system, total number of moles remains constant.
So.
Initially, $p_{1} V=n_{1} R T_{1}$ and $p_{2} V=n_{2} R T_{2}$
then, $\mathrm{p}(2 \mathrm{~V})=\left(\mathrm{n}_{1}+\mathrm{n}_{2}\right) \mathrm{RT}$
$\therefore \frac{p}{T}=\frac{\left(n_{1}+n_{2}\right)}{2 V} R=\frac{1}{2}\left(\frac{p_{1}}{T_{1}}+\frac{p_{2}}{T_{2}}\right)$
$=\frac{1}{2}\left(\frac{p_{1} T_{2}+p_{2} T_{1}}{T_{1} T_{2}}\right)$
20. At room temperature the nns speed of the molecules of a certain diatomic gas is found to be $1930 \mathrm{~m} / \mathrm{s}$; the gas is:
a) hydrogen
b) fluorine
c) oxygen
d) chlorine
21. The mean kinetic energy of the mole of gas per degree of freedom (on the basis of Kinetic theory of gases ) is ;
a) $\frac{1}{2} \mathrm{kT}$
b) $\frac{3}{2} \mathrm{kT}$
c) $\frac{3}{2} \mathbf{k T}$
d) $\frac{1}{2} \mathrm{RT}$
22. 10,000 small balls, each weighing 1 g , strike one square em of area per second with a velocity $100 \mathrm{~m} / \mathrm{s}$ in a normal direction and rebound with the same velocity. The value of pressure on the surface will be:
a) $2 \times 10^{3} \mathrm{~N} / \mathrm{m}^{2}$
b) $2 \times 10^{5} \mathrm{~N} / \mathrm{m}^{2}$
c) $10^{7} \mathrm{~N} / \mathrm{m}^{2}$
d) $\mathbf{2 \times 1 0 ^ { 7 }} \mathrm{N} / \mathrm{m}^{2}$

## Solution : -

Change in momentum of one ball $=2 \mathrm{mv}=2 \times 1 \times 10^{-3} \times 100$ Rate of change of momentum $=$ force i.e., $F=2 \times 1 \times 10^{-3} \times 100 \times 10,000=2 \times 10^{3} \mathrm{~N}$

Pressure $=\frac{F}{A}=\frac{2 \times 10^{3}}{1 \times 10^{-4}}=2 \times 10^{7} \mathrm{~N} / \mathrm{m}^{2}$
23. The root mean square and most probable speed of the molecules in a gas are:
a) same
b) different
c) cannot say
d) depends on nature of the gas
24. Half a mole of helium at $27^{\circ} \mathrm{C}$ and at a pressure of 2 atmosphere is mixed with I .5 mole of Nj at $77^{\circ} \mathrm{C}$ and at a pressure at 5 atmosphere so that the volume of the mixture is equal to the sum of their initial volumes. If the temperature of the mixture is $69^{\circ} \mathrm{C}$, its pressure is:
a) 3.5 atm
b) 3.8 atm
c) 3.95 atm
d) 4.25 atm

## Solution:-

$P_{1} V_{1}=u_{1} R T_{1}$
or $\mathrm{V}_{1}=\frac{u_{1} R T_{1}}{P_{1}}=\frac{1}{2} \frac{R(300)}{2}=75 R$
$\mathrm{P}_{2} \mathrm{~V}_{2}=\mathrm{u}_{2} \mathrm{RT}_{2}$
or $\mathrm{V}_{2}=\mathrm{u} 2 \frac{R T_{2}}{P_{2}}=1.5 \frac{R(350)}{5}=105 R$
$\mathrm{P}\left(\mathrm{V}_{1}+\mathrm{V}_{2}\right)=\left(\mathrm{u}_{1}+\mathrm{u}_{2}\right) \mathrm{Rt}$
or $\mathrm{P}(75 \mathrm{R}+105 \mathrm{R})=\left(\frac{1}{2}+1.5\right) \mathrm{R}(273+69)$
or $\mathrm{P} \times 180 \mathrm{R}=2 \times \mathrm{R} \times 342$
$\mathrm{P}=\frac{342}{90}=3.8 \mathrm{~atm}$
25. Equal volume of monoatomic and diatomic gases at the same temperature are given equal quantities of heat.

Then:
a) the temperature of diatomic gas will be more
b) the temperature of monoatomic gas will be more
c) the temperature of both will be zero
d) nothing can be said

## Solution : -

Since, monoatomic gas has one degree of freedom, so rise of temperature will be more in its case.
26. A gas is heated through $1^{\circ} \mathrm{C}$ in a closed vessel. Its pressure is increased by $0.4 \%$. The initial temperature of the gas is:
a) $250^{\circ} \mathrm{C}$
b) $100^{\circ} \mathrm{C}$
c) $-75^{\circ} \mathrm{C}$
d) $-23^{\circ} \mathrm{C}$

## Solution:-

$\mathrm{T}_{1}=\mathrm{T} ; \mathrm{P}_{1}=\mathrm{P}$
$\mathrm{P}_{2}=0.4 \%$ more than $\mathrm{P}_{1}=\mathrm{P}+\frac{0.4 P}{100}=\frac{100.4 \mathrm{P}}{100}$
So, $\frac{P_{1} V_{1}}{T_{1}}=\frac{P_{2} V_{2}}{T_{2}}$
$\frac{P V}{T}=\frac{100.4 P}{100} \cdot \frac{V}{T+1}$
Solving, we get; $\mathrm{T}=250 \mathrm{~K}=-23^{\circ} \mathrm{C}$.
27. The root mean square speed of hydrogen molecules at a certain temperature is $300 \mathrm{~m} / \mathrm{s}$. If the temperature is doubled and hydrogen gas dissociates into atomic hydrogen, the rms speed will become:
a) 424.26 mls
b) $300 \mathrm{~m} / \mathrm{s}$
c) $\mathbf{6 0 0 ~ M} / \mathrm{s}$
d) $150 \mathrm{M} / \mathrm{s}$

Solution : -
$v_{r m s}=\sqrt{\frac{3 R T}{M}}$
T is doubled and M is halved. Thereforce, rms speed will become two times or $600 \mathrm{~m} / \mathrm{s}$.
28. For a gas, $\frac{R}{C_{V}}=0.67$, the gas is made up of molecules which are
a) monoatomic
b) diatomic
c) triatomic
d) polyatomic

## Solution:-

$\frac{R}{C_{V}}=067=\frac{2}{3} \Rightarrow C_{V}=\frac{3}{2} R$
So, the gas must be monoatomic.
29. The average kinetic energy of a gas molecule is:
a) proportional to pressure of gas
b) inversely proportional to volume of gas
c) inversely proportional to absolute temperature of gas
d) proportional to absolute temperature of gas
30. If the masses of all molecules of a gas are halved and their speeds doubled, then the ratio of initial and final pressures would be
a) $2: 1$
b) $1: 2$
c) 4 : 1
d) $1: 4$

## Solution :

$P=\frac{1}{3} \frac{m N}{V} v^{2}, \quad p^{\prime}=\frac{1}{3} \frac{(m / 2) N}{v}(2 \bar{v})^{2}$
$\therefore \frac{P^{\prime}}{P}=\frac{2}{1}$ or $\frac{P}{P^{\prime}}=1: 2$
31. Three perfect gases at absolute temperatures $T_{1}, T_{2}$ and $T_{3}$ are mixed. The masses of molecules are $m_{1}, m_{2}$ and $m_{3}$ and the number of molecules are $n_{1}, n_{2}$ and $n_{3}$ respectively. Assuming no loss of energy, the final temperature of the mixture is:
a) $\frac{\left(T_{1}+T_{2}+T_{3}\right)}{3}$
b) $\frac{n_{1} T_{1}+n_{2} T_{2}+n_{3} T_{3}}{n_{1}+n_{2}+n_{3}}$
c) $\frac{n_{1} T_{1}^{2}+n_{2} T_{2}^{2}+n_{3} T_{3}^{2}}{n_{1} T_{1}+n_{2} T_{2}+n_{3} T_{3}}$
d) $\frac{n_{1}^{2} T_{1}^{2}+n_{2}^{2} T_{2}^{2}+n_{3}^{2} T_{3}^{2}}{n_{1} T_{1}+n_{2} T_{2}+n_{3} T_{3}}$
32. A balloon contains $1500 \mathrm{~m}^{3}$ of helium at $27^{\circ} \mathrm{C}$ and 4 atmospheric pressure. The volume of helium at $-3^{\circ} \mathrm{C}$ temperature and 2 atmospheric pressure will be:
a) $1500 \mathrm{~m}^{3}$
b) $1700 \mathrm{~m}^{3}$
c) $1900 \mathrm{~m}^{3}$
d) $\mathbf{2 7 0 0} \mathrm{m}^{\mathbf{3}}$

## Solution : -

$\mathrm{V}_{1}=1500 \mathrm{~m}^{3}, \mathrm{~T} 1=27^{\circ} \mathrm{C}=300 \mathrm{~K}$
$\mathrm{P}_{1}=4 \mathrm{~atm}, \mathrm{~T}_{2}=-3^{\circ} \mathrm{C}=270 \mathrm{~K}$
$\mathrm{P}_{2}=2 \mathrm{~atm}$
$\frac{P_{1} V_{1}}{T_{1}}=\frac{P_{2} V_{2}}{T_{2}}$
$\therefore V_{2}=\frac{P_{1} V_{1}}{T_{1}} \times \frac{T_{2}}{P_{2}}=\frac{4 \times 1500 \times 270}{300 \times 20} 2700 \mathrm{~m}^{3}$.
33. A sealed container with negligible thermal coefficient of expansion contains helium (a monoatomic gas). When it is heated from 300 K to 600 K , the average kinetic energy of helium atoms is:
a) halved
b) left unchanged
c) doubled
d) increases by a factor of $\sqrt{2}$
34. A bubble is at the bottom of the lake of depth $h$. As the bubble comes to sea level, its radius increases three times. If atmospheric pressure is equal to 1 metres of water column, then h is equal to:
a) 26 I
b) I
c) 25 I
d) 301

## Solution : -

From Boyle's law $\mathrm{p}_{\mathrm{V}}=$ constant
$\therefore \mathrm{p}_{1} \mathrm{~V}_{1}=\mathrm{p}_{2} \mathrm{~V}_{2}$
Here, $\mathrm{p}_{1}=(\mathrm{h}+1), \mathrm{V}_{1}=\frac{4}{3} \pi r^{3}$
$\mathrm{p}_{2}=\mathrm{I}, \mathrm{V}_{2}=\frac{4}{3} \pi(3 r)^{3}$
$\therefore(\mathrm{h}+\mathrm{I}) \frac{4}{3} \pi r^{3}=\mathrm{Ix} \frac{4}{3} \pi(3 r)^{3}$
or $\mathrm{h}+\mathrm{l}=27 \mathrm{l} . \mathrm{h}=26 \mathrm{l}$
35. Let $\bar{v}, \bar{v}$ and $\mathrm{v}_{\mathrm{p}}$ respectively denote the mean speed, root mean square speed and most probable speed of the molecules in an ideal monoatomic gas at absolute temperature T . The mass of the molecule is m . Then:
a) No molecules can have a speed greater than $\left(\sqrt{2} v_{r m s}\right)$
b) No molecules can have a speed less than $\frac{v_{p}}{(\sqrt{2})}$
c) $\bar{v}<\mathrm{v}_{\mathrm{p}}<\mathrm{v}_{\mathrm{rms}}$
d) the average kinetic energy of the molecules is $\frac{3}{4}\left(m v_{p}^{2}\right)$

## Solution : -

$v_{r m s}=\sqrt{\frac{3 R T}{m}}$
$\bar{v}=\sqrt{\frac{8 R T}{\pi m}}=\sqrt{\frac{2.5 R T}{m}}$
and $\mathrm{vp}=\sqrt{\frac{2 R T}{m}}$

Form these expressions, we can see that
$v_{p}<\bar{v}<v_{r m s}$
Again, $v_{r m s}=v_{p} \sqrt{\frac{3}{2}}$
and average kinetic energy of a gas molecule
$\mathrm{Ek}=\frac{1}{2} \mathrm{mv}^{2}$
$\mathrm{Ek}=\frac{1}{2} m\left(\sqrt{\frac{3}{2}} v_{p}\right)^{2}=\frac{1}{2} m \times \frac{3}{2} v_{p}^{2}=\frac{3}{4} m v v_{p}^{2}$
36. The gas in a vessel is subjected to a pressure of 20 atmosphere at a temperature $27^{\circ} \mathrm{C}$. The pressure of the gas in the vessel after one half of the gas is released from the vessel and the temperature of the remainder is raised by, $50^{\circ} \mathrm{C}$, is:
a) 8.5 atm
b) 10.8 atm
c) 11.67 atm
d) 17 atm

## Solution:-

$\mathrm{PV}=\frac{m}{M} \mathrm{RT}$
$20 \times \mathrm{V}=\frac{m}{M} R \times 300, P^{\prime} \times V=\frac{(m /)}{M} R \times 350$
$\therefore \mathrm{P}^{\prime}=\frac{140}{12}=11.67 \mathrm{~atm}$.
37. Some gas at 300 K is enclosed in a container. Now, the container is placed on a fast moving train. While the train is in motion, the temperature of the gas:
a) rises above 300 K
b) falls below 300 K
c) remains unchanged
d) becomes unsteady

Solution : -
Random motion of molecules and not ordered motion causes rise of temperature.
38. What is an ideal gas?
a) One that consists of molecules
b) A gas satisfying the assumptions of kinetic theory
c) A gas having Maxwellian distribution of speed
d) A gas consisting of massless particles
39. The root mean square velocity of the molecules of a gas is $1260 \mathrm{~m} / \mathrm{s}$. The average speed of the molecules is
a) $1029 \mathrm{~ms}^{-1}$
b) $1161 \mathrm{~ms}^{-1}$
C) $1671 \mathrm{~ms}^{-1}$
d) $917 \mathrm{~ms}^{-1}$

## Solution:-

$\mathrm{v} \mathrm{av}=\sqrt{\frac{8 k Y}{m \pi}}, \mathrm{vrms}=\sqrt{\frac{3 k T}{m}}$
$\therefore \frac{v_{a v}}{v_{r m p}}=\frac{\sqrt{8 / \pi}}{\sqrt{3}}$
or $\frac{v_{a v}}{1260}=\sqrt{\frac{8}{3 \pi}}$
$\therefore \mathrm{v}_{\mathrm{av}}=1260 \times \sqrt{\frac{8}{3 \pi}}=1161 \mathrm{~ms}^{-1}$.
40. On any planet, the presence of atmosphere implies; ( $\mathrm{v}_{\mathrm{rms}}=$ root mean square velocity of molecules and $\mathrm{v}_{\mathrm{e}}=$ escape velocity))
a) $v_{r m s} \ll v_{e}$
b) $u_{r m s}>v_{e}$
c) $\mathrm{v}_{\mathrm{rms}}=\mathrm{v}_{\mathrm{e}}$
d) $v_{\text {rms }}=0$
41. If $C_{8}$ be the velocity of sound in air and $C$ be the rms velocity, then:
a) $\mathrm{Cs}<\mathrm{C}$
b) $\mathrm{Cs}=\mathrm{C}$
c) $\mathbf{C s}=\mathbf{C} \sqrt{\gamma / 3}$
d) none of these
42. The root mean square velocity, vrms, the avaerage velocity, $\mathrm{v}_{\mathrm{av}}$ and the most probable velocity, $\mathrm{v}_{\mathrm{mp}}$ of the molecules of the gas are in the order:
a) $v_{m p}>v_{a v}>v_{r m s}$
b) $\mathrm{v}_{\mathrm{rms}}>\mathrm{v}_{\mathrm{av}}>\mathrm{v}_{\mathrm{mp}}$
c) $\mathrm{vav}>\mathrm{v}_{\mathrm{mp}}>\mathrm{v}_{\mathrm{rms}}$
d) $v_{\mathrm{mp}}>\mathrm{v}_{\mathrm{rms}}>\mathrm{v}_{\mathrm{av}}$

## Solution:-

$v_{r m s}=\sqrt{\frac{3 K T}{m}}, v_{a v}=\sqrt{\frac{8 K T}{m \pi}}$
and $v_{m p}=\sqrt{\frac{2 K T}{m}}$
$\therefore \mathrm{v}_{\mathrm{rms}}>\mathrm{v}_{\mathrm{av}}>\mathrm{v}_{\mathrm{mp}}$
43. IF both the temperature and the volume of an ideal gas are doubled, the pressure:
a) Increases by a factor of 4
b) is also doubled
c) remains unchanged
d) is diminshed by a factor $\frac{1}{4}$
44. If the pressure of an ideal gas contained in a closed vessel increased by $0.5 \%$, the increase in temperature is 2

K . The initial temperature of the gas is:
a) $27^{\circ} \mathrm{C}$
b) $127^{\circ} \mathrm{C}$
c) $300^{\circ} \mathrm{C}$
d) $400^{\circ} \mathrm{C}$
45. At what temperature the molecules of nitrogen will have the same rms velocity as the molecules of oxygen a $127^{0}$ C
a) $77^{\circ} \mathrm{C}$
b) $350^{\circ} \mathrm{C}$
c) $273^{\circ} \mathrm{C}$
d) $457^{\circ} \mathrm{C}$
46. A real gas behaves like an ideal gas if its:
a) pressure and temperature are both high
b) pressure and temperature are both low
c) pressure is high and temperature is low
d) pressure is low and temperature is high
47. A vessel contains a mixture of Imole of oxygen and 2 moles of nitrogen at 300 K . The ratio of average rotational kinetic energy per $\mathrm{O}_{2}$ molecule to that of per $\mathrm{N}_{2}$ molecule is:
a) $1: 1$
b) $1: 2$
c) $2: 1$
48. An insulated box containing a diatomic gas of molar mass $M$ is moving with a velocity $u$. The box is suddenly stopped. The resulting change in temperature is:
a) $\frac{m v^{2}}{2 R}$
b) $\frac{m v^{2}}{3 R}$
c) $\frac{m v^{2}}{5 R}$
d) $\frac{2 m v^{2}}{5 R}$
49. In an ideal gas without preferred direction of motion molecules,
a) None of the above
b) $v_{x}=v_{y}=v_{z}$
c) $v_{x}^{2}=v_{x}^{y}=v_{z}^{2}$
d) $\bar{v}_{x}^{2}=\bar{v}_{y}^{2}=\bar{v}_{z}^{2}$

## Solution:-

An isotropic gas is one which have same properties throughout and their molecules are all moving in random direction, so only average of square of their velocity components are equal.
50. By what percentage should the pressure of a given mass of a gas be increased so as to decrease its volume by $10 \%$ at a constant temperature?
a) $8.1 \%$
b) $9.1 \%$
c) $10.1 \%$
d) $11.1 \%$

## Solution :-

$\frac{P V}{T}=\frac{p^{\prime} \times \frac{90}{100} V}{T}$
$\therefore \frac{P^{\prime}}{P}=\frac{100}{90}=1+\frac{10}{90}$
$\therefore \frac{P^{\prime}-P}{P}=\frac{10}{90} \times 100=11.1 \%$

